

Physics 4062/5062 –Tutorial 2 – Polarization

Linearly Polarized

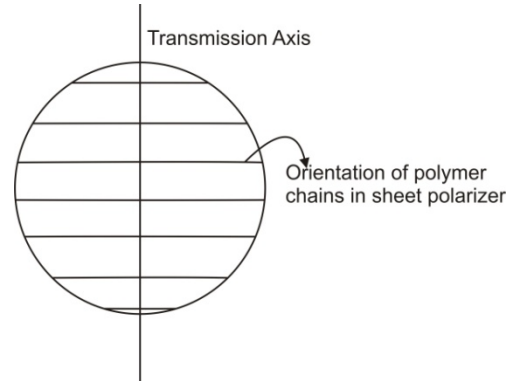
- E field measured in plane perpendicular to direction of propagation
- **E** orientation constant
- $|\mathbf{E}|$ and sign vary with time
- Eg: Laser Output
- Consider polarizer oriented at angle θ to vertical

$$\mathbf{E}_y = E_o \cos\theta \text{ is transmitted}$$

$$I_T \propto E_o^2 \cos^2\theta = I_o \cos^2\theta \rightarrow \text{transmission function}$$

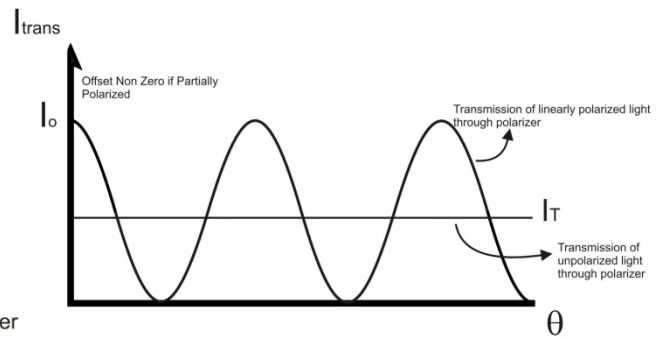
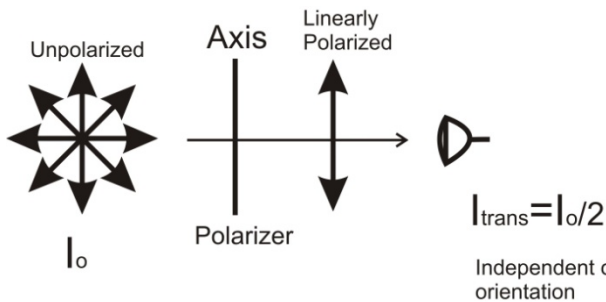
- Note that the plane polarized or linearly polarized light can be represented as the sum of two orthogonally polarized components that have the same phase

$$\mathbf{E} = (\hat{x}E_{ox} - \hat{y}E_{oy}) \cos(kz - wt)$$



Unpolarized Light

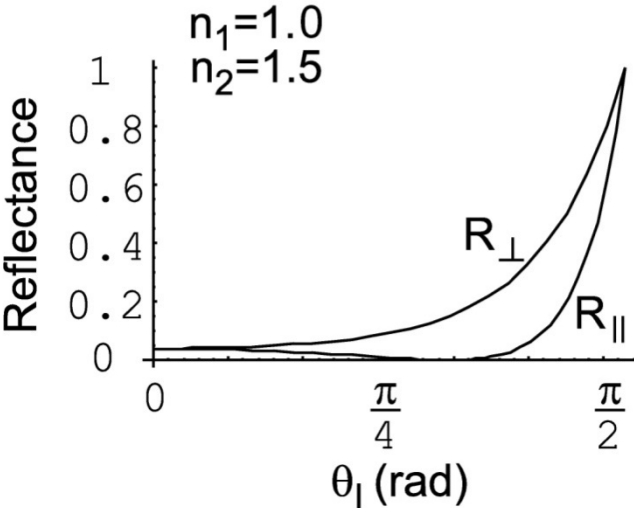
- Eg: Light Bulb
- superposition of linear polarizations with randomly varying phase



- On Average, equal amounts of linearly polarized light transmitted at all polarizer orientations θ , so that $I_T = I_o/2$

Polarization by Reflection

- Light reflected differently depending on polarization



Circular Polarization

$$E_{oy} = E_{ox}$$

- Circular polarization can be represented as the superposition of two phase shifted linearly polarized components
- Combination of two perpendicular E fields with 90 degree phase shift
- Likewise, linear polarization can be expressed as the sum of two opposite circular polarizations

Wave plates

$\lambda/4$	$\delta = 90^\circ$	$d n_{\perp} - n_{\parallel} = \lambda/4$
$\lambda/2$	$\delta = 180^\circ$	$d n_{\perp} - n_{\parallel} = \lambda/2$
Λ	$\delta = 360^\circ$	$d n_{\perp} - n_{\parallel} = \lambda$

- n_{\perp} and n_{\parallel} are indices of refraction perpendicular and parallel to the optic axis of the wave plate
- Difference in phase velocities along these directions produces a phase shift

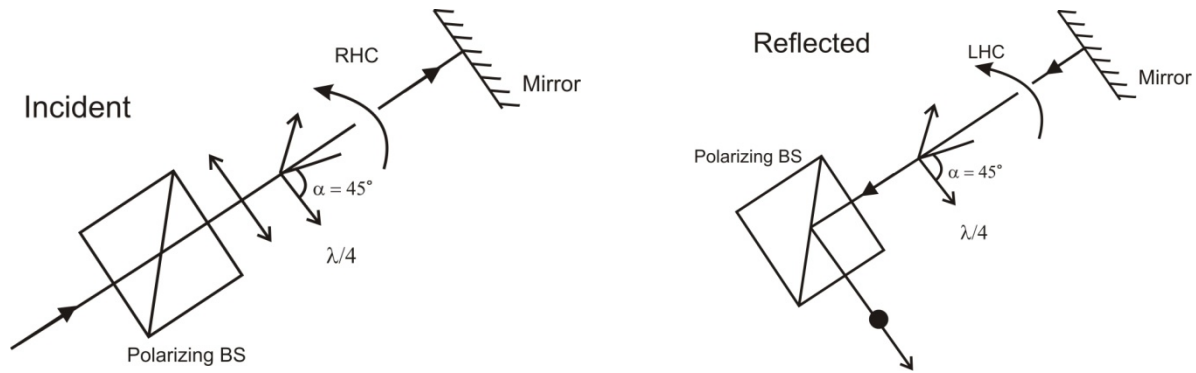
Effect of Quarter Wave Plate on Linearly Polarized Light

1. $\alpha = \pm 45^\circ$ (RHC and LHC), where α is angle of optic axis of wave plate with plane of polarization
 - Represent incident light as sum of two orthogonal linearly polarized components
 - E field components parallel and perpendicular to optic axis are phase shifted by $\delta = \pi/2$
 - after $\lambda/4 \Rightarrow$ result is circularly polarized light
2. $\alpha = 0^\circ$ or 90°
 - No effect
 - Linearly polarized output
3. $\alpha \neq 45^\circ, 0^\circ$ or 90°
 - Elliptically polarized output

Half Wave plate

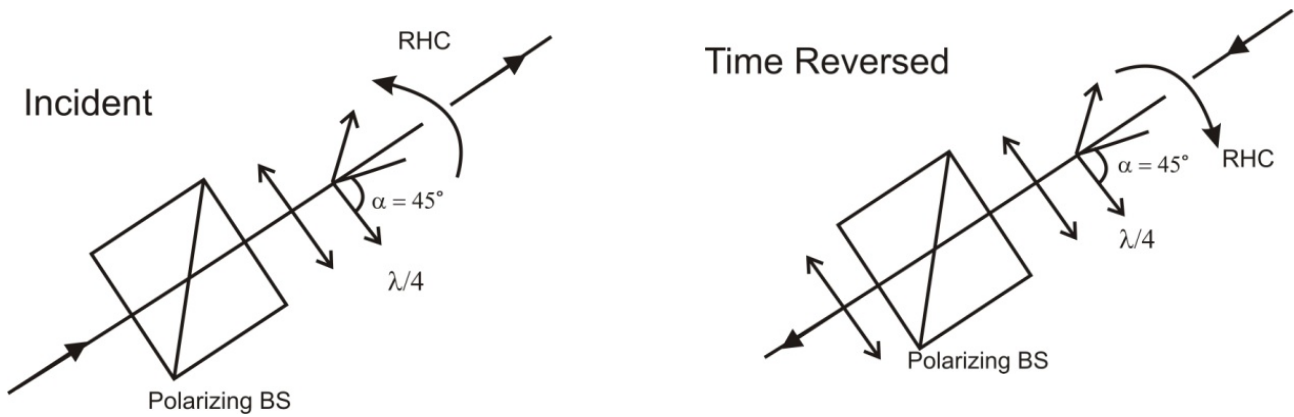
- two quarter wave plates with $\alpha_1 = \alpha_2 = 45^\circ$
- $\delta = \delta_1 + \delta_2 = \pi$, which corresponds to a path difference of $\lambda/2$

Mirror Reversal



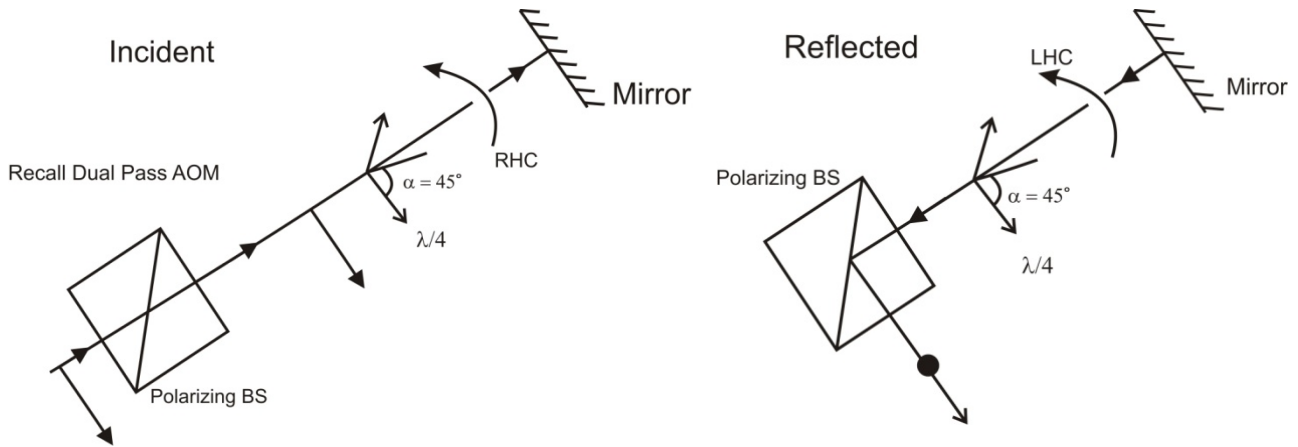
- No change in angular momentum of light \mathbf{L}
- No transfer of angular momentum to mirror
- Change in polarization - RHC changes to LHC

Time Reversal (different from mirror reversal)



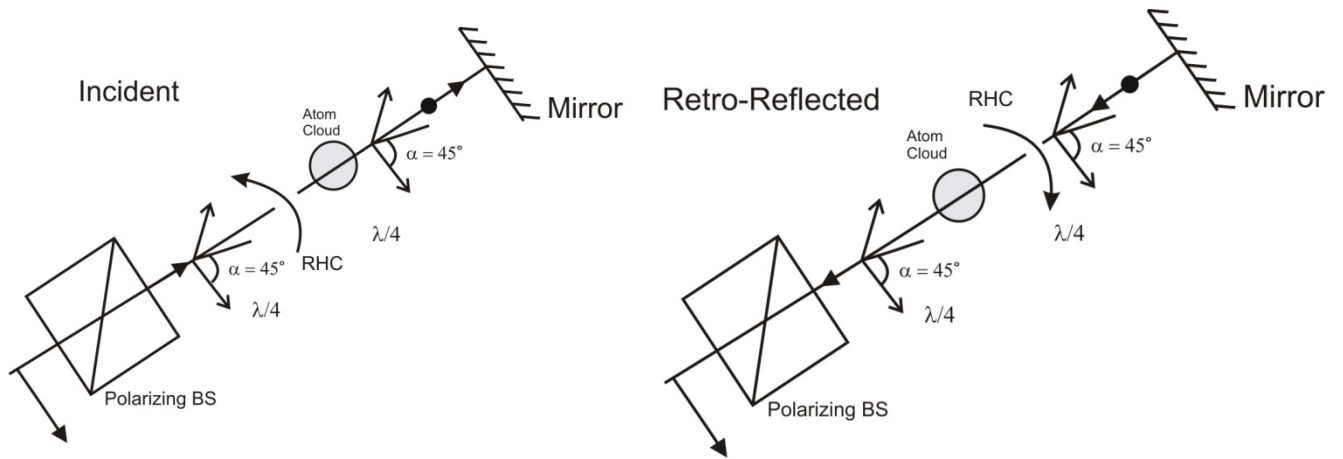
- Change in angular momentum
- No change in outgoing polarization
- Angular momentum unchanged

Standing Wave Case



Retro-Reflected Beams for Atom Trap

- opposite angular momentum
- Need σ^+ and σ^-



The second QWP is shown identical to the first QWP. However, σ^+ (incident) and σ^- (retro) beams will be produced for any orientation of the second QWP.

Assume that incident is σ^+ and Reflected light is σ^-